



Test Examination: Mechatronics and Electrical Drives

08.01.2014

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Course of Study:																																				
Exercise:	1	2	3						Total																											
(Points)	(20)	(20)	(20)						(60)																											

Duration: 90 Minutes

Permitted:

- a self-created, handwritten sheet of formulas (1 sheet A4, inscribed on one side, no copies or prints)
- a non-programmable calculator without graphic display
- drawing materials (compasses, protractor, ruler, pens ...)

Please bring your student ID card (with photo)!

Please label each exam sheet with your name and student number. Use for each task a new exam sheet. Do not use pencils or red pens.

All solutions must be clearly documented and wherever required explained! The entry of a mere final result without any approach will not be counted.

Good Luck!

Exercise 1: Basic Magnetics

(20 Points)

For the circuit shown in Figure. 1, calculate the following , when the voltage source V_s has a voltage waveform as shown in figure 2. (Neglect the winding resistance, μ_r of the core is 10,000 and other parameters are given in the figure. neglect the fringing effects and assume that all the flux generated links both the windings)

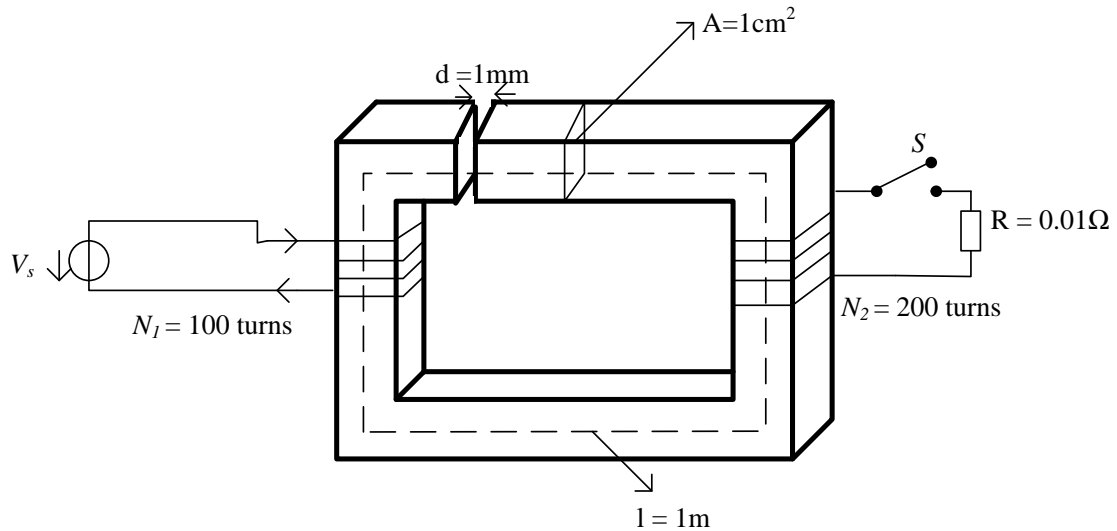


Figure. 1

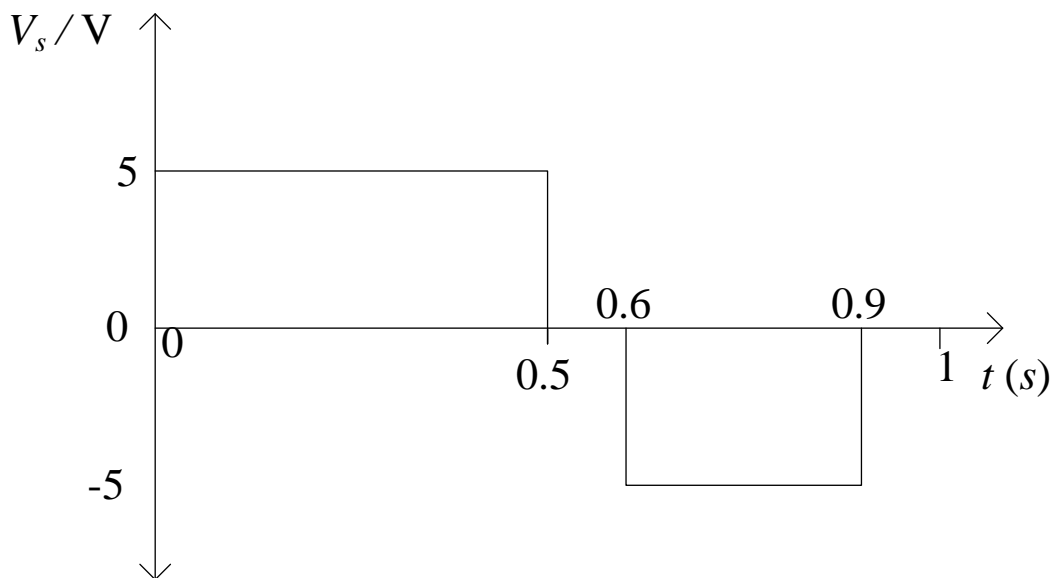


Figure. 2 input voltage waveform

1.1 For the case, with switch S open:

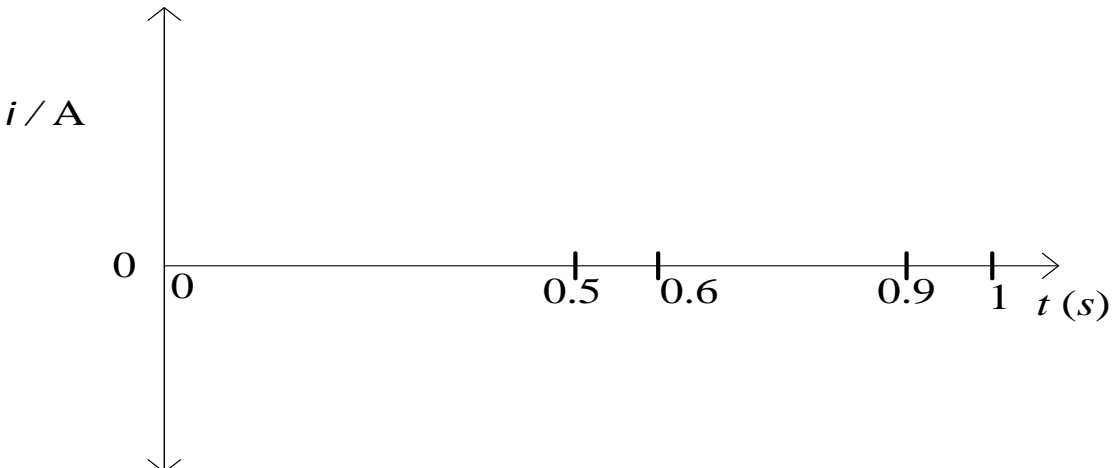
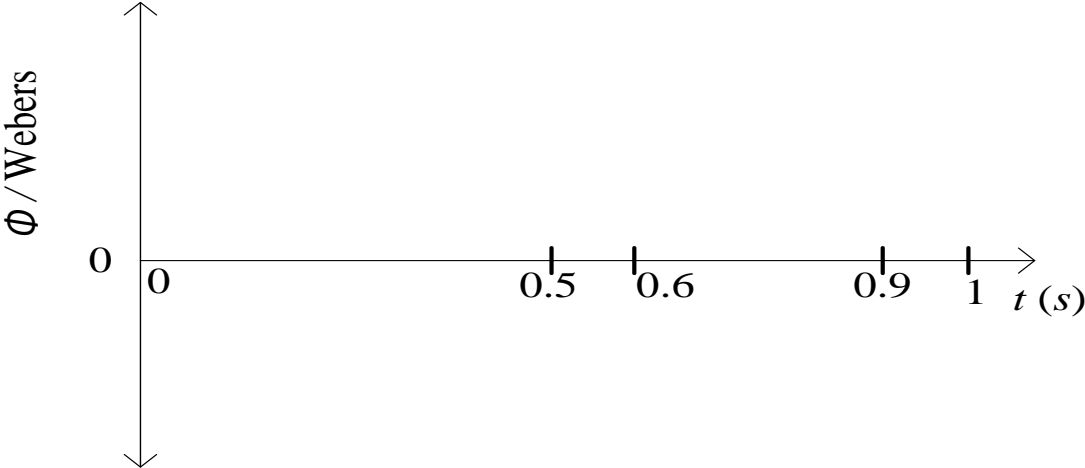
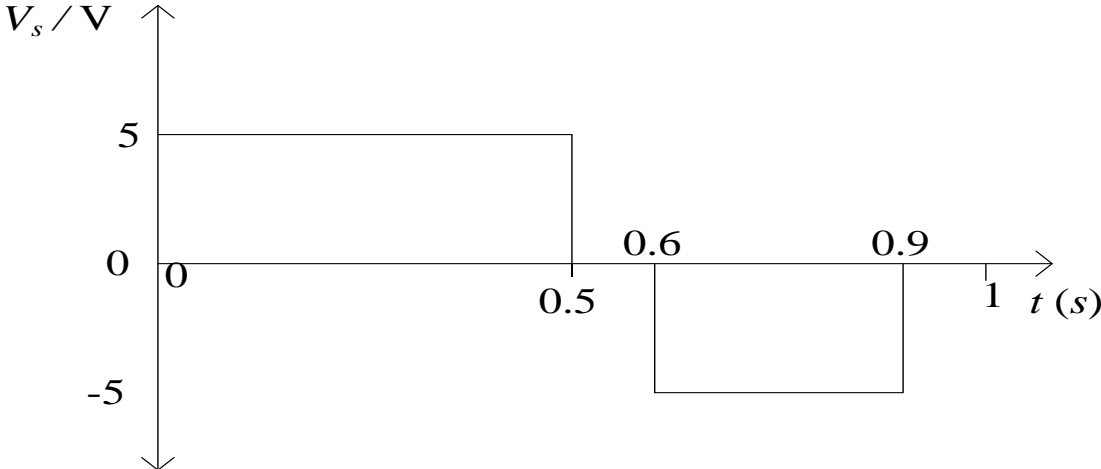
a) Calculate the inductance when seen from the primary side (left hand side).

- b) Draw the waveform of flux in the core and the primary current waveform, from time $t = 0$ s to $t = 1$ s. Please use the sheets provided for drawing these waveforms
- c) Calculate the value of flux density at the end of 200 ms

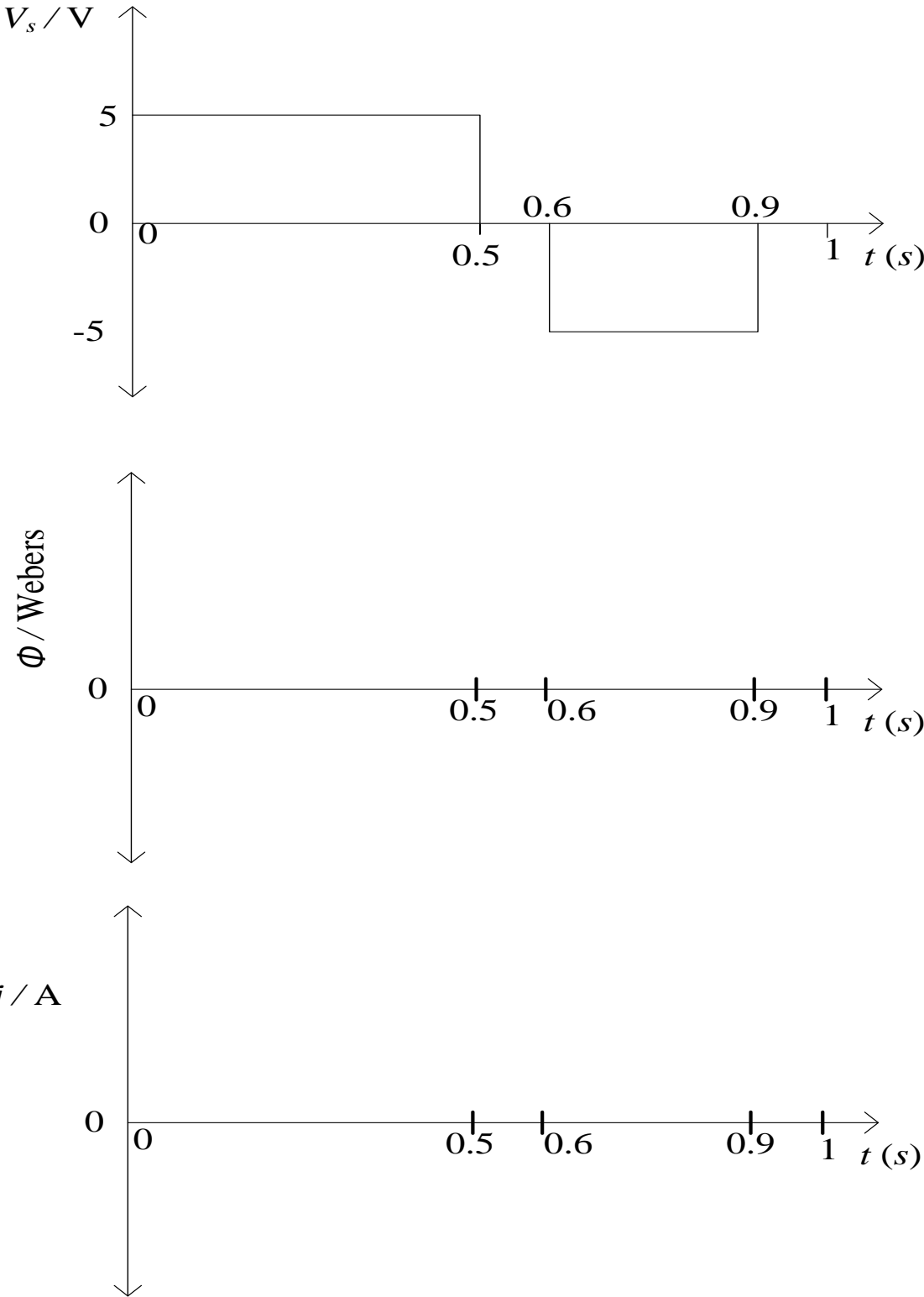
1.2 For the case, with switch S closed:

- a) Calculate the inductance when seen from the primary side (left hand side).
- b) Draw the waveform of flux in the core and the primary current waveform, from time $t = 0$ s to $t = 1$ s. Please use the sheets provided for drawing these waveforms.
- c) Calculate the value of flux density in the core at the end of 200 ms.

Answer 1.1: For the case, with switch S open

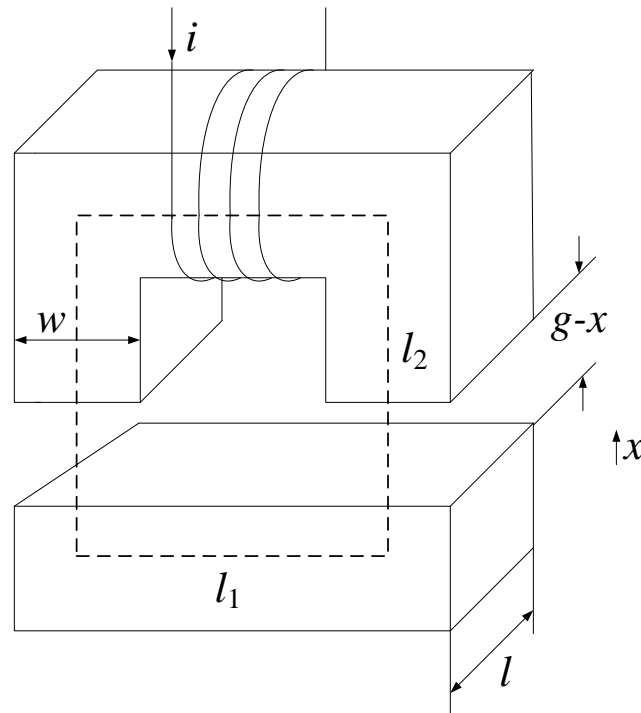


Answer 1.2: For the case, with switch S closed,



Exercise 2: Magnetic Bearing
(20 Points)

Figure below depicts an electromagnet used to suspend an I-shaped core with a magnetic force. The C-core has a width w and a length l . The main flux path is indicated by a dotted line. The length of the flux paths in the C and I-cores are represented by l_1 and l_2 . The winding has N turns with the current value as i . The airgap length is g at the nominal position. At a displacement $x \ll g$, as shown in the figure, obtain the following:



- 2.1** Assume the core permeability to be μ_r . Evaluate the various reluctances and obtain the equivalent magnetic circuit.
- 2.2** Now consider the cores to be ideal ($\mu_r = \infty$). Evaluate the various reluctances with this assumption and obtain the following:

Hint: Use $\frac{1}{g-x} = \frac{1}{g} \left(1 + \frac{x}{g}\right)$ for $x \ll g$, wherever required

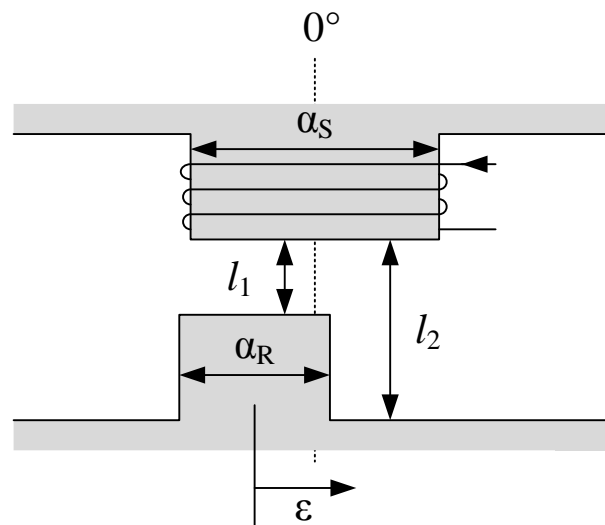
- The flux linkage in the coil
- Inductance of the coil
- Flux density in the air-gap
- Energy and Co-energy
- Force experienced by the I-core. Indicate the direction of force. How can the direction of the force be reversed?
- Is the system inherently stable? Explain. If not, how can the system be stabilized? Explain.

Exercise 3: Reluctance Motor
(20 Points)

The figure below depicts a segment of a reluctance motor. The lower rotor pole is moving at a constant speed under an energized stator pole. The dimensions of the air gap are $l_1 = 1 \text{ mm}$ and $l_2 = 2.5 \text{ mm}$. The dimensions of the motor are listed as:

$$\alpha_S = 50^\circ, \alpha_R = 25^\circ, A_S = 800 \text{ mm}^2, A_R = 400 \text{ mm}^2, i = 35 \text{ A}, N = 10$$

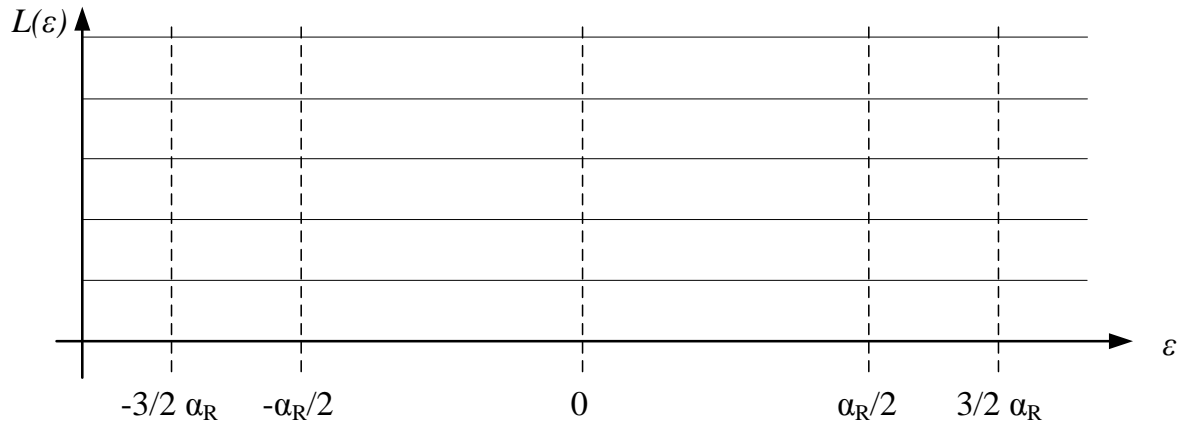
Note: Assume that the magnetic field is oriented in the vertical direction. The reluctance the stator and rotor iron can be neglected.



3.1 Set up the equations for the air-gap reluctance as a function of the angle ϵ :

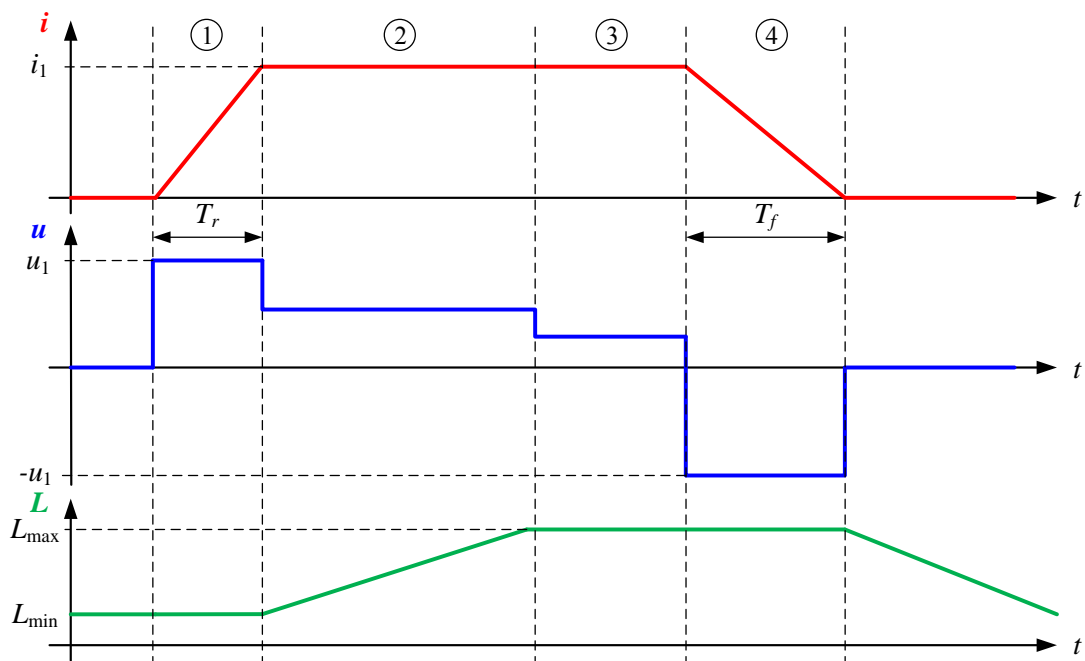
- in the non-aligned position ($\epsilon = \alpha$)
- in the fully aligned position ($\epsilon = 0^\circ$)
- during transition ($-3/2 \alpha_R < \epsilon < -\alpha_R/2$)
- Sketch the variation of the air gap reluctance for a complete electrical cycle.

3.2 Calculate the torque and sketch the variation of inductance as a function of the angle ϵ in the graph on the next page.



The following questions are independent of the machine configuration and can be answered without results from the previous task!

- 3.3 a) Explain the following characteristic curves of a reluctance motor for the different sub-intervals 1, 2, 3 and 4.



- b) Calculate the magnetization and demagnetization times T_r and T_f , with the following values:
 $u_1 = 250 \text{ V}$, $i_1 = 35 \text{ A}$, $L_{\min} = 1 \text{ mH}$, $L_{\max} = 2,75 \text{ mH}$

Note: The ohmic resistance can be neglected.

- 3.4 Is material with a non-linear magnetization behavior in a reluctance motor advantageous? Give reasons for your answer!
- 3.5 Why does an asymmetric half-bridge converter instead of a four quadrant converter enough for supplying a reluctance motor? Explain.